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# The microstructure parameters and microhardness of directionally solidified Ti-43Al-3Si alloy

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#### A R T I C L E I N F O

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#### 1. Introduction

Intermetallic  $\gamma$ -TiAl-based alloys are considered to be a new generation of high temperature structural materials for aerospace and automotive industries due to their low density, good oxidation resistance and high temperature strength [1–4]. Of the numerous microstructures that can be formed in TiAl-based alloys, the fully lamellar microstructures consisting of TiAl ( $\gamma$ -phase) and Ti<sub>3</sub>Al ( $\alpha_2$ -phase) have displayed a good combination of room temperature toughness, ductility, creep strength and elevated temperature strength [5,6].

As was shown in the literature [5,7–10], TiAl-based alloys with aligned lamellar orientation have a good combination of strength and ductility in a wide range of temperature. The main challenge is that the lamellar microstructure is not form from the liquid but from the solid-state transformation [5,7–10]. During cooling the  $\gamma$  phases form from the matrix  $\alpha$  phases according to the crystallographic orientation relationship of  $(111)_{\gamma}//(0001)_{\alpha}$ . Due to the preferred growth direction of  $\alpha$  phase is [0001], the lamellar orientation is perpendicular to the growth direction. Hence, to obtain the preferred lamellar orientation, the orientation of high temperature  $\alpha$  phase must first be controlled [8–11]. However, the aligned lamellar orientation can be obtained by directional solidification and seeding techniques with a seed having specific  $\alpha$  orientation [7,9,11–14,5]. One of the main factors for this tech-

#### ABSTRACT

TiAl-based alloy (Ti-43Al-3Si at.%) was directionally solidified at a constant temperature gradient (*G* = 20 K/mm) in a wide range of growth rates (5–60 µm/s) by using a Bridgman type directional solidification furnace. The cellular spacing ( $\lambda$ ), lamellar spacing ( $\lambda_L$ ), volume fraction of Ti<sub>5</sub>Si<sub>3</sub> phases (*f<sub>V</sub>*) and microhardness (*H<sub>V</sub>*) were measured. The values of  $\lambda$ ,  $\lambda_L$  and *f<sub>V</sub>* decrease with increasing growth rate (*V*). The value of *H<sub>V</sub>* increases with the increasing values of *V* and  $\lambda_L^{-0.5}$ , and decreases with the increasing values of  $\lambda$ , and *f<sub>V</sub>*. The dependence of *H<sub>V</sub>* on *V*,  $\lambda_L^{-0.5}$  and *f<sub>V</sub>* was determined by linear regression analysis. The fitted exponent values obtained in this work were compared with the previous experimental results for similar alloy systems.

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nique is to found a suit seeding materials. As a seed material, the primary solidification phase must be  $\alpha$  phase and the original lamellar orientation should be restored during heating to and cooling from single-phase  $\alpha$ -region [8,14]. According to the literature [5,7,9,12,15], Ti-43Al-3Si(at.%) alloy is identified to be a suitable seed material which is used to control the orientation of lamellar structures in TiAl alloys. However, the evolution of microstructure characteristics for Ti-43Al-3Si(at.%) alloy during directional solidification has not been well understood. The microstructure characteristics of Ti-43Al-3Si(at.%) alloy are important to the controlling of lamellar orientation of TiAl-based alloys during directional solidification. Unfortunately, little work has been reported about the microstructure characteristics of directionally solidified Ti-43Al-3Si(at.%) alloy.

As reported by Lapin et al. [6,15], there is a linear relationship between microhardness and yield stress, which promises the mechanical properties of directionally solidified TiAl ingots to be predicted from the values of Vickers microhardness. Similar linear dependence of the yield stress on the hardness was also observed in wrought TiAl alloy with fully lamellar structures [16]. It appears that the microhardness analysis offers a relatively simple method to predict the mechanical properties of materials [17]. The values of Vickers microhardness are useful for quality control in the production of directionally solidified TiAl alloys.

The purpose of this work is to study the evolution of microstructure characteristics and microhardness for Ti-43Al-3Si(at.%) alloy during directional solidification. In this paper, directionally solidified Ti-43Al-3Si(at.%) alloy has been carried out to experimentally investigate the effect of growth rate (V) on the cellular spacing

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Fig. 1. Schematic of Bridgman type directional solidification furnace.

( $\lambda$ ), interlamellar spacing ( $\lambda_L$ ) and volume fraction of Ti<sub>5</sub>Si<sub>3</sub> phases ( $f_V$ ) during the directional solidification. The dependences of the microhardness ( $H_V$ ) on the growth rate (V), cellular spacing ( $\lambda$ ), interlamellar spacing ( $\lambda_L$ ) and volume fraction of Ti<sub>5</sub>Si<sub>3</sub> phases ( $f_V$ ) are also studied.

#### 2. Experimental procedures

Master ingot with nominal composition of Ti-43Al-3Si(at%) alloy was prepared by using Ti (99.96%), Al (99.99%) and Si (99.96%) of commercial purity in a cold crucible induction furnace under argon atmosphere. The samples were machined to rods with 3 mm diameter and 100 mm in length from the ingot by a spark machining. The directional solidification (DS) experiments were performed in Bridgman-type system. The schematic diagram of Bridgman type directional solidification furnace is shown in Fig. 1. The apparatus consisted of an induction coil, a graphite heater, a water cooled liquid metal bath filled with a liquid Ga-In-Sn alloy and an adiabatic zone which is located between the heater and the cooler. The temperature gradient was measured by W/Re thermocouples that were placed near the outside surface of the alumina tubes, as shown in Fig. 1. The temperature gradient close to the solid/liquid interface was measured to be approximately 20 K/mm. The samples are placed into 99.99 pct pure alumina crucibles of 4/5.5 mm diameter (insider/outside diameter) and length of 150 mm. Each specimen was heated to 1723 K during 4 h and held for different time before directional solidification, and then was directionally solidified with growth rate range from 5  $\mu$ m/s to 60  $\mu$ m/s. The growth length of the samples is 40 mm during directional solidification. At the end of the experiment, the sample was guenched into the liquid Ga-In-Sn alloy to restored the solid/liquid interface.

After directional solidification, the longitudinal and transverse section of the specimens were cut, polished and etched with a solution of 10 ml HF- $10 \text{ ml HON}_3$ - $180 \text{ ml H}_2\text{O}$  for further analysis. After metallographic process, the microstructures of the samples were revealed and photographed with optical microscope. Fig. 2 shows the typical images of optical microscope.

The cellular spacings were measured from the photographs according to the method described in Refs. [18,19]. The interlamellar spacings were measured from the SEM back scattered electron (BSE) images according to the method described in Ref. [20]. The value of interlamellar spacing is the thickness of one  $\alpha$  lamellae and  $\gamma$  lamellae nearby. Fig. 2 shows the typical BSE images of lamellar structures. The measured values are the average values and given in Table 1.

Microhardness measurements were made with a standardized Vickers measuring test device using 100 g load and a dwell time of 10 s on the longitudinal section. The microhardness is average of at least 15 measurements. The values of  $H_V$  are also given in Table 1.

#### 3. Results and discussion

#### 3.1. Microstructure of directionally solidified ingots

The microstructure of the directionally solidified specimen consisted of  $\alpha_2(Ti_3AI)/\gamma(TiAI)$  lamellar structures and  $\xi$ -Ti<sub>5</sub>Si<sub>3</sub> phases, as shown in Fig. 2. The chemical composition analysis of the phases in the samples was carried out by using energy dispersive X-ray analysis (EDX) and is given in Fig. 3. According to EDX results and the solubility of components in phase, the black phases are  $\gamma$  phase, the gray ones are  $\alpha_2$  phase and the white are Ti<sub>5</sub>Si<sub>3</sub> phase. Fig. 4 shows the calculated partial isopleth diagram of Ti-Al-Si ternary system at 3.5 at.% Si after Manesh and Flower [21]. The lamellar structures formed by eutectoid reaction:  $\alpha \rightarrow \alpha_2 + \gamma$ . Due to the low solubility of Si in the matrix, some isolated large Ti<sub>5</sub>Si<sub>3</sub> rods formed in the Si-rich region of the liquid phase by reaction of  $L \rightarrow \xi$ . The eutectic Ti<sub>5</sub>Si<sub>3</sub> phase formed by reaction:  $L \rightarrow \alpha + \xi$  and  $L \rightarrow \gamma + \xi$ , as described in Ref. [22]. In addition, some Al<sub>2</sub>O<sub>3</sub> particles that formed by the reaction between the crucible and the alloy were observed in the directionally solidified specimens, which were shown in Fig. 2(a2, c2 and d2). The solid-liquid interface and microstructure evolution of Ti-43Al-3Si(at.%) alloy was studied in previous works [22,23].

## 3.2. Effect of growth rate on the cellular spacing, the interlamellar spacing and volume fraction of Ti<sub>5</sub>Si<sub>3</sub> phases

Fig. 5 shows the variations of the cellular spacing ( $\lambda$ ), interlamellar spacing ( $\lambda_L$ ) and volume fraction of Ti<sub>5</sub>Si<sub>3</sub> phases ( $f_V$ ) with the growth rate (V) at a constant temperature gradient (G = 20 K/mm). The error bars indicate the errors in the  $\lambda$  values,  $\lambda_L$  values and  $f_V$  values, which are in the range of ±2%, ±2.5% and ±2%. The values of  $\lambda$ ,  $\lambda_L$  and  $f_V$  decrease with the increasing the values of Vat constant G. The value of  $f_V$  decreases from 12.2 to 8.9 pct with increasing growth rate (V) from 5 µm/s to 60 µm/s at constant G. The largest  $f_V$  (12.5%) was obtained at the growth rate (V = 10 µm/s), which is greater than the value of 9.3% obtained by Sun et al. [24] for Ti-48Al-3Si(at.%) alloy. The relationship between  $\lambda$ ,  $\lambda_L^{-0.5}$ ,  $f_V$ and V was obtained by using linear regression analysis, the results were given as:

$$\lambda = 650.1 \, V^{-0.44} \tag{1}$$

$$\lambda_L = 13.2 \, V^{-0.41} \tag{2}$$

$$f_V = 16.6 \, V^{-0.17} \tag{3}$$

The regression coefficient of this fit is  $r^2 = 0.97$ , 0.99 and 0.87, respectively.

The exponent value of growth rate (*V*) for  $\lambda$  was fitted to be 0.44 that is small than the theoretical value of 0.5, 0.5 and 0.59 resulting from the model of Okamoto–Kishitake [25], Bouchard–Kirkaldy [26] and Hunt–Lu [27], respectively. However, the exponent value is greater the theoretical value of 0.25 from the models of Hunt [28], Kruz–Fisher [29], Kruz–Fisher [30] and Trivedi Model [31], respectively. The exponent value of interlamellar spacing is greater than 0.24 obtain by Lapin et al. [6] for Ti–46Al–2W–0.5Si(at.%) alloy.

The volume fraction of  $Ti_5Si_3$  phase decrease with increasing growth. It is because that the rejection of solute was restrained with increasing growth rate, which cause the decreasing of the concentration of Si in the liquid phase. Therefore, the formation of  $Ti_5Si_3$  phase was reduced and the volume fraction of  $Ti_5Si_3$  phase decreased.

# 3.3. Dependency of the microhardness on the growth rate, cellular spacing, lamellar spacing and volume fraction of $Ti_5Si_3$ phase

Fig. 6 shows the variations of the microhardness ( $H_V$ ) with the growth rate (V), cellular spacing ( $\lambda$ ), lamellar spacing ( $\lambda_L$ ) and volume fraction of Ti<sub>5</sub>Si<sub>3</sub> ( $f_V$ ) phases at a constant temperature gradient (G = 20 K/mm). The error bars indicate the errors in the values of  $H_V$ ,  $\lambda$  and  $f_V$ , which are in the range of ±1%, ±2% and ±2%, respectively. The value of  $H_V$  increases with the increasing the values of V at constant G, as shown in Fig. 6a. The value of  $H_V$  increases with the



**Fig. 2.** Images of growth morphologies of directionally solidified Ti-43Al-3Si(at.%) alloy with different growth rates in constant temperature gradient (G=20K/mm): (a) V=5  $\mu$ m/s; (b) V=10  $\mu$ m/s; (c) V=20  $\mu$ m/s; (d) V=30  $\mu$ m/s; (e) V=60  $\mu$ m/s. The left sides are corresponded to optical images of longitudinal section at solid-liquid interface; right sides corresponded to BSE images of transverse section, respectively. The arrows indicate the Al<sub>2</sub>O<sub>3</sub> particles.

### 596 **Table 1**

The values of cellular spacing, lamellar spacing and microhardness for directionally solidified Ti-43Al-3Si(at.%) alloy at various growth rate with constant temperature gradient (G=20K/mm).

Solidification parameters		Cellular spacing	Lamellar spacing	Volume fraction of Ti <sub>5</sub> Si <sub>3</sub> phases	Microhardness
G(K/mm)	V(µm/s)	λ (μm)	$\lambda_L (\mu m)$	f <sub>V</sub> (%)	$H_V$
20	5	371.7	6.88	12.2	420.4
	8	210.7	5.41	11.8	434.6
	10	238.2	5.31	12.5	460.7
	15	192.0	4.68	11.4	479.8
	20	187.3	3.76	9.1	496.3
	25	169.0	3.44	10.2	480.8
	30	133.8	3.34	8.1	503.2
	40	135.8	2.67	9.1	524.2
	50	100.4	2.71	8.8	512.1
	60	120.0	2.54	8.9	549.4

![](_page_3_Figure_4.jpeg)

Fig. 3. The chemical composition analysis of Ti-43Al-3Si(at.%) alloy by using SEM EDX, the black phases are  $\gamma$ -TiAl phase, the grey phases are  $\alpha_2$ -Ti<sub>3</sub>Al phase, the white phases are  $\xi$ -Ti<sub>5</sub>Si<sub>3</sub> phase.

![](_page_4_Figure_1.jpeg)

**Fig. 4.** The calculated partial isopleth diagram of Ti–Al–Si ternary system at 3.5 at.% Si after Manesh and Flower [22].

increasing the value of  $\lambda_L^{-0.5}$ , according to a Hall–Petch type relationship in the form of  $H_V = H_{V0} + k\lambda_L^{-0.5}$  [6,16,32], where  $H_{V0}$  and k are materials constants. It was found that the value of  $H_V$  decreases with increasing  $\lambda$  and  $f_V$ . The dependence of the  $H_V$  on V,  $\lambda$ ,  $\lambda_L^{-0.5}$  and  $f_V$  was determined by using linear regression analysis, and the

results were given as:

$$H_V = 363.1 \, V^{0.10} \tag{4}$$

 $H_V = 1288.2\lambda^{-0.19} \tag{5}$ 

$$H_V = 257.5 + 0.44\lambda_L^{-0.5} \tag{6}$$

$$H_V = 1318.3 f_V^{-0.44} \tag{7}$$

The regression coefficients are  $r^2 = 0.96$ , 0.90, 0.95, and 0.83, respectively.

The exponent value of growth rate (*V*) is 0.10 that is in smaller than the value of 0.14 and 0.15 obtained by Lapin et al. [6] for Ti-46Al-2W-0.5Si(at.%) alloy and Fan et al. [33] for Ti-46Al-0.5W-0.5Si(at.%) alloy, respectively. The exponent value of cellular spacing ( $\lambda$ ) is 0.19 that is smaller than the value of 0.31 obtained by Fan et al. [33] for Ti-46Al-0.5W-0.5Si(at.%) alloy.

With increasing of the growth rate, the cellular spacing ( $\lambda$ ) decreased and the columnar grains were refined. The strength of the directionally solidified Ti–43Al–3Si(at.%) was enhanced by fine grains. Consequently, the microhardness ( $H_V$ ) increased with decreased cellular spacing ( $\lambda$ ). During the directional solidification, element of Si rejected in the liquid phase between the dendrites due to the low solubility of Si in the  $\alpha_2/\gamma$  lamellar structures. The Ti<sub>5</sub>Si<sub>3</sub> phase formed in the Si-rich region of the liquid by the reaction of by L  $\rightarrow$  Ti<sub>5</sub>Si<sub>3</sub>. With increasing growth rate, the cooling rate increased and the rejection of Si was restrained. Hence, the volume fraction ( $f_V$ ) of Ti<sub>5</sub>Si<sub>3</sub> phase decreased. The concentration of Si in the  $\alpha_2/\gamma$  lamellar structures increased, which has solution strengthen effect for the Ti–43Al–3Si(at.%) alloy. Therefore, the microhardness ( $H_V$ ) increased with decreased of  $f_V$ .

![](_page_4_Figure_12.jpeg)

Fig. 5. Effects of growth rate on the cellular spacing (a), the lamellar spacing (b) and the volume fraction of Ti<sub>5</sub>Si<sub>3</sub> phases (c) of directionally solidification Ti–43Al–3Si(at.%) alloy at a constant temperature gradient (*G*=20 K/mm).

![](_page_5_Figure_1.jpeg)

**Fig. 6.** The variation of microhardness as a function of growth rate (a), cellular spacing (b), reciprocal square root of interlamellar spacing (c), and volume fraction of Ti<sub>5</sub>Si<sub>3</sub> phases (d) for directionally solidification Ti-43Al-3Si(at.%) alloy at a constant temperature gradient (*G* = 20 K/mm).

#### 4. Conclusions

In the present work, the microstructure parameters and microhardness of directionally solidified Ti-43Al-3Si(at.%) alloy were investigated. The following conclusions were reached:

(1) The values of cellular spacing  $(\lambda)$ , interlamellar spacing  $(\lambda_L)$  and volume fraction of  $(f_V)$  alloy decrease with increasing growth rate (V) for directionally solidified Ti-43Al-3Si(at.%). The relationships were given as follows:

$$\begin{split} \lambda &= 650.1 \, V^{-0.44} \\ \lambda L &= 13.2 \, V^{-0.41} \\ f_V &= 16.6 \, V^{-0.17}. \end{split}$$

(2) The valuable of microhardness ( $H_V$ ) increases with increasing growth rate (V) and the reciprocal square root of interlamellar spacing ( $\lambda_L^{-0.5}$ ) for directionally solidified Ti–43Al–3Si(at.%) alloy. The relationships can be given as:

$$\begin{split} H_V &= 363.1 \, V^{0.10} \\ H_V &= 257.5 + 0.44 \lambda L^{-0.5}. \end{split}$$

(3) The valuable of microhardness ( $H_V$ ) decreases with increasing cellular spacing ( $\lambda$ ) and volume fraction of Ti<sub>5</sub>Si<sub>3</sub> phase ( $f_V$ ) for directionally solidified Ti-43Al-3Si(at.%) alloy. The relationships were given as:

 $H_V = 1288.2\lambda^{-0.19}$  $H_V = 1318.3 f_V^{-0.44}.$ 

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